



Design Approach for the Folded-Cascode Op Amp

Step	Relationship	Design Equation/Constraint	Comments
1	Slew Rate	$I_3 = SR \cdot C_L$	
2	Bias currents in output cascodes	$I_4 = I_5 = 1.2I_3$ to $1.5I_3$	Avoid zero current in cascodes
3	Maximum output voltage, $v_{out(max)}$	$S_5 = \frac{2I_5}{K_P \cdot V_{SD5}^2}$, $S_7 = \frac{2I_7}{K_P \cdot V_{SD7}^2}$, ($S_4 = S_5$ and $S_6 = S_7$)	$V_{SD5(sat)} = V_{SD7(sat)} = 0.5[V_{DD} - V_{out(max)}]$
4	Minimum output voltage, $v_{out(min)}$	$S_{11} = \frac{2I_{11}}{K_N \cdot V_{DS11}^2}$, $S_9 = \frac{2I_9}{K_N \cdot V_{DS9}^2}$, ($S_{10} = S_{11}$ and $S_8 = S_9$)	$V_{DS9(sat)} = V_{DS11(sat)} = 0.5[V_{out(min)} - V_{SS}]$
5	$GB = \frac{g_{m1}}{C_L}$	$S_1 = S_2 = \frac{g_{m1}^2}{K_N \cdot I_3} = \frac{GB^2 C_L^2}{K_N \cdot I_3}$	
6	Minimum input CM	$S_3 = \frac{2I_3}{K_N \cdot (V_{in(min)} - V_{SS} - \sqrt{(I_3/K_N \cdot S_1)} - V_{T1})^2}$	
7	Maximum input CM	$S_4 = S_5 = \frac{2I_4}{K_P \cdot (V_{DD} - V_{in(max)} + V_{T1})^2}$	S_4 and S_5 must meet or exceed value in step 3
8	Differential Voltage Gain	$\frac{v_{out}}{v_{in}} = \left(\frac{g_{m1}}{2} + \frac{g_{m2}}{2(1+k)} \right) R_{out} = \left(\frac{2+k}{2+2k} \right) g_{m1} R_{out}$	$k = \frac{R_{II}(g_{ds2} + g_{ds4})}{g_{m7} r_{ds7}}$
9	Power dissipation	$P_{diss} = (V_{DD} - V_{SS})(I_3 + I_{10} + I_{11})$	

Example 6.5-3 Design of a Folded-Cascode Op Amp

Follow the procedure given to design the folded-cascode op amp when the slew rate is $10\text{V}/\mu\text{s}$, the load capacitor is 10pF , the maximum and minimum output voltages are $\pm 2\text{V}$ for $\pm 2.5\text{V}$ power supplies, the GB is 10MHz , the minimum input common mode voltage is -1.5V and the maximum input common mode voltage is 2.5V . The differential voltage gain should be greater than $5,000\text{V}/\text{V}$ and the power dissipation should be less than 5mW . Use channel lengths of $1\mu\text{m}$.

Solution

Following the approach outlined above we obtain the following results.

$$I_3 = SR \cdot C_L = 10 \times 10^6 \cdot 10^{-11} = 100\mu\text{A}$$

Select $I_4 = I_5 = 125\mu\text{A}$.

Next, we see that the value of $0.5(V_{DD} - V_{out(\text{max})})$ is $0.5\text{V}/2$ or 0.25V . Thus,

$$S_4 = S_5 = \frac{2 \cdot 125\mu\text{A}}{50\mu\text{A}/\text{V}^2 \cdot (0.25\text{V})^2} = \frac{2 \cdot 125 \cdot 16}{50} = 80$$

and assuming worst case currents in M6 and M7 gives,

$$S_6 = S_7 = \frac{2 \cdot 125\mu\text{A}}{50\mu\text{A}/\text{V}^2 (0.25\text{V})^2} = \frac{2 \cdot 125 \cdot 16}{50} = 80$$

The value of $0.5(V_{out(\text{min})} - |V_{SS}|)$ is also 0.25V which gives the value of S_8, S_9, S_{10} and

$$S_{11} \text{ as } S_8 = S_9 = S_{10} = S_{11} = \frac{2 \cdot I_8}{K_N' V_{DS8}^2} = \frac{2 \cdot 125}{110 \cdot (0.25)^2} = 36.36$$

In step 5, the value of GB gives S_1 and S_2 as

$$S_1 = S_2 = \frac{GB^2 \cdot C_L^2}{K_N' I_3} = \frac{(20\pi \times 10^6)^2 (10^{-11})^2}{110 \times 10^{-6} \cdot 100 \times 10^{-6}} = 35.9$$

The minimum input common mode voltage defines S_3 as

$$S_3 = \frac{2I_3}{K_N' \left(V_{in(\text{min})} - V_{SS} - \sqrt{\frac{I_3}{K_N' S_1}} - V_{T1} \right)^2} = \frac{200 \times 10^{-6}}{110 \times 10^{-6} \left(-1.5 + 2.5 - \sqrt{\frac{100}{110 \cdot 35.9}} - 0.7 \right)^2} = 91.6$$

We need to check that the values of S_4 and S_5 are large enough to satisfy the maximum input common mode voltage. The maximum input common mode voltage of 2.5 requires

$$S_4 = S_5 \geq \frac{2I_4}{K_P' [V_{DD} - V_{in(\text{max})} + V_{T1}]^2} = \frac{2 \cdot 125\mu\text{A}}{50 \times 10^{-6} \mu\text{A}/\text{V}^2 [0.7\text{V}]^2} = 10.2$$

which is much less than 80 . In fact, with $S_4 = S_5 = 80$, the maximum input common mode voltage is 3V .

The power dissipation is found to be

$$P_{diss} = 5\text{V}(125\mu\text{A} + 125\mu\text{A}) = 1.25\text{mW}$$

Example 6.5-3 - Continued

The small-signal voltage gain requires the following values to evaluate:

$$S_4, S_5: g_m = \sqrt{2 \cdot 125 \cdot 50 \cdot 80} = 1000 \mu\text{S} \quad \text{and} \quad g_{ds} = 125 \times 10^{-6} \cdot 0.05 = 6.25 \mu\text{S}$$

$$S_6, S_7: g_m = \sqrt{2 \cdot 75 \cdot 50 \cdot 80} = 774.6 \mu\text{S} \quad \text{and} \quad g_{ds} = 75 \times 10^{-6} \cdot 0.05 = 3.75 \mu\text{S}$$

$$S_8, S_9, S_{10}, S_{11}: g_m = \sqrt{2 \cdot 75 \cdot 110 \cdot 36.36} = 774.6 \mu\text{S} \quad \text{and} \quad g_{ds} = 75 \times 10^{-6} \cdot 0.04 = 3 \mu\text{S}$$

$$S_1, S_2: g_{mI} = \sqrt{2 \cdot 50 \cdot 110 \cdot 35.9} = 628 \mu\text{S} \quad \text{and} \quad g_{ds} = 50 \times 10^{-6} (0.04) = 2 \mu\text{S}$$

Thus,

$$R_{II} \approx g_{m9} r_{ds9} r_{ds11} = (774.6 \mu\text{S}) \left(\frac{1}{3 \mu\text{S}} \right) \left(\frac{1}{3 \mu\text{S}} \right) = 86.07 \text{M}\Omega$$

$$R_{out} \approx 86.07 \text{M}\Omega \parallel (774.6 \mu\text{S}) \left(\frac{1}{3.75 \mu\text{S}} \right) \left(\frac{1}{2 \mu\text{S} + 6.25 \mu\text{S}} \right) = 19.40 \text{M}\Omega$$

$$k = \frac{R_{II}(g_{ds2} + g_{ds4})}{g_{m7} r_{ds7}} = \frac{86.07 \text{M}\Omega (2 \mu\text{S} + 6.25 \mu\text{S}) (3.75 \mu\text{S})}{774.6 \mu\text{S}} = 3.4375$$

The small-signal, differential-input, voltage gain is

$$A_{vd} = \left(\frac{2+k}{2+2k} \right) g_{mI} R_{out} = \left(\frac{2+3.4375}{2+6.875} \right) 0.628 \times 10^{-3} \cdot 19.40 \times 10^6 = 7,464 \text{ V/V}$$

The gain is larger than required by the specifications which should be okay.