

This time waveform can be written as a Fourier Series because it is periodic with period T and amplitude A.

$$f(t) = \frac{A}{2} + \sum_{n \text{ odd}}^{\infty} \frac{2A}{n\pi} \sin(2n\pi t)$$

Using Eulers Formula :

$$\sin(2n\pi t) = \frac{e^{j2n\pi t} - e^{-j2n\pi t}}{2}$$
$$A \sin(2n\pi t) = \frac{A}{2} (e^{j2n\pi t} - e^{-j2n\pi t})$$

$$P = \frac{1}{T} \int_0^T x(t)^2 dt = \frac{1}{T} \int_0^T \{A \sin(2n\pi t)\}^2 dt$$
$$= \frac{A^2}{T} \int_0^T \{\sin(2n\pi t)\}^2 dt$$

$$\int_0^T \{\sin(at)\}^2 dt = \left( \frac{t}{2} \right) - \left( \frac{\sin(2at)}{4a} \right)$$

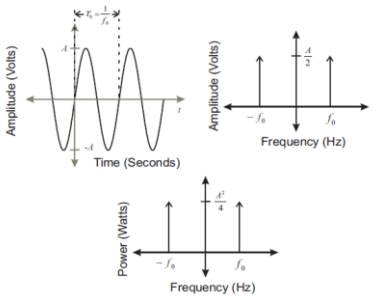
$$\frac{A^2}{T} \int_0^T \{\sin(2n\pi t)\}^2 dt = \frac{A^2}{T} \left\{ \left( \frac{T}{2} \right) - \left( \frac{\sin(4n\pi t)}{8n\pi} \right) \right\}$$

$$= \frac{A^2}{T} \left\{ \left( \frac{T}{2} \right) - \left( \frac{\sin(4n\pi T)}{8n\pi} \right) \right\}$$

$$= \frac{A^2}{T} \left\{ \left( \frac{T}{2} \right) - \left( \frac{\sin(4n\pi)}{8n\pi} \right) \right\}$$

for n is odd  
 $\sin(4n\pi) = 0$

$$= \frac{A^2}{T} \left\{ \left( \frac{T}{2} \right) \right\}$$
$$= \frac{A^2}{2}$$



## 50% DUTY CYCLE

To provide a normalised response the Fourier coefficient for f(1) = 1 i.e. multiply by  $n/2 \cdot A$

AMPLITUDE A = 1		HARMONIC	AVERAGE POWER		PEAK VOLTAGE 1 line spectra	dB <sub>u</sub> 1 line spectra	PEAK VOLTAGE 2 line spectra	AVERAGE POWER (WATTS) 2 line spectra	dB <sub>w</sub> 2 line spectra	dB <sub>u</sub> 2 line spectra	DIFF dB <sub>u</sub>	NORMALISATION	
				(WATTS) 1 line spectra									
f(t) = $\frac{A}{2}$		n = 0	0.5	0.25	23.9794009		0.5	0.25	-6.0206	23.979400	0	0.79	27.901798
f(t) = $\frac{A}{2}$	"+"	$\frac{2 \cdot A}{\pi} \sin(2\pi ft)$	n = 1	0.636620	0.202642	23.0673025	0.318310	0.1013221184	-9.943	20.057003	3.0103 i.e. multiply by 2	1.00	30
		n = 2	0					0		0.000000	-3.0103	5.00E-04	
f(t) = $\frac{A}{2}$	"+"	$\frac{2 \cdot A}{3\pi} \sin(6\pi ft)$	n = 3	0.212207	0.022516	13.52487741	0.106103	0.011257909	-19.4854	10.514577		1/3	0.33
		n = 4											
f(t) = $\frac{A}{2}$	"+"	$\frac{2 \cdot A}{5\pi} \sin(10\pi ft)$	n = 5	0.127324	0.008106	9.087902416	0.063662	0.004052847	-23.9224	6.077602		1/5	0.20
		n = 6	0					0					
f(t) = $\frac{A}{2}$	"+"	$\frac{2 \cdot A}{7\pi} \sin(14\pi ft)$	n = 7	0.090946	0.004136	6.165341702	0.045473	0.002067779	-26.845	3.155042		1/7	0.14
		n = 8	0					0		0.000000			
f(t) = $\frac{A}{2}$	"+"	$\frac{2 \cdot A}{9\pi} \sin(18\pi ft)$	n = 9	0.070736	0.002502	3.982452314	0.035368	0.001250879	-29.0278	0.972152		1/9	0.11
		n = 10	0					0		0.000000			
f(t) = $\frac{A}{2}$	"+"	$\frac{2 \cdot A}{11\pi} \sin(22\pi ft)$	n = 11	0.057875	0.001675	2.2394488	0.028937	0.000837365	-30.7709	-0.770851		1/11	0.09
		n = 12	0					0		0.000000			
f(t) = $\frac{A}{2}$	"+"	$\frac{2 \cdot A}{13\pi} \sin(26\pi ft)$	n = 13	0.048971	0.001199	0.788435457	0.024485	0.000599534	-32.2219	-2.221865		1/13	0.08
									-172.216	61.76306			

0.4502775  
**CORRECT !!!!**

0.371387497  
**CORRECT !!!!**  
-4.30172721 dB<sub>w</sub>

This is the power in watts only upto n=13 if we let n = ∞ the total power = 0.5 W.

$$P = \frac{1}{T} \int_0^T x(t)^2 dt$$
$$P = \frac{1}{T} \int_0^T (1)^2 dt = 0.5 \text{ W}$$

	dB <sub>u</sub> 1 line spectra		dB <sub>u</sub> 2 line spectra
0.000000	23.979400	0	23.9794
2000	23.0673025	1	20.0570
	0	2	0.0000
6000	13.52487741	3	10.5146
	0	4	0.0000
10000	9.087902416	5	6.0776
	0	6	0.0000
14000	6.165341702	7	3.1550
	0	8	0.0000
18000	3.982452314	9	0.9722
	0	10	0.0000
20000	2.2394488	11	-0.7709
	0	12	0.0000
24000	0.788435457	13	-2.2219
0	23.97940009		23.9794
2000	23.0673025		20.057
6000	13.52487741		10.51458
10000	9.087902416		6.077602
14000	6.165341702		3.155042
18000	3.982452314		0.972152
20000	2.2394488		-0.770851
24000	0.788435457		-2.221865